## Lesson 12: Linear Equations in Two Variables

## Classwork

## Opening Exercise

Emily tells you that she scored 32 points in a basketball game. Write down all the possible ways she could have scored 32 with only two- and three-point baskets. Use the table below to organize your work.

| Number of Two-Pointers | Number of Three-Pointers |
| :--- | :--- |
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Let $x$ be the number of two-pointers and $y$ be the number of three-pointers that Emily scored. Write an equation to represent the situation.

## Exploratory Challenge/Exercises

1. Find five solutions for the linear equation $x+y=3$, and plot the solutions as points on a coordinate plane.

| $\boldsymbol{x}$ | Linear Equation: <br> $x+y=3$ | $\boldsymbol{y}$ |
| :--- | :--- | :--- |
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2. Find five solutions for the linear equation $2 x-y=10$, and plot the solutions as points on a coordinate plane.

| $\boldsymbol{x}$ | Linear Equation: <br> $2 x-y=10$ | $\boldsymbol{y}$ |
| :--- | :--- | :--- |
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3. Find five solutions for the linear equation $x+5 y=21$, and plot the solutions as points on a coordinate plane.

| $\boldsymbol{x}$ | Linear Equation: <br> $x+5 y=21$ | $\boldsymbol{y}$ |
| :--- | :--- | :--- |
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4. Consider the linear equation $\frac{2}{5} x+y=11$.
a. Will you choose to fix values for $x$ or $y$ ? Explain.
b. Are there specific numbers that would make your computational work easier? Explain.
c. Find five solutions to the linear equation $\frac{2}{5} x+y=11$, and plot the solutions as points on a coordinate plane.

| $\boldsymbol{x}$ | Linear Equation: $\frac{2}{5} x+y=11$ | $y$ |
| :---: | :---: | :---: |
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5. At the store, you see that you can buy a bag of candy for $\$ 2$ and a drink for $\$ 1$. Assume you have a total of $\$ 35$ to spend. You are feeling generous and want to buy some snacks for you and your friends.
a. Write an equation in standard form to represent the number of bags of candy, $x$, and the number of drinks, $y$, that you can buy with $\$ 35$.
b. Find five solutions to the linear equation from part (a), and plot the solutions as points on a coordinate plane.

| $\boldsymbol{x}$ | Linear Equation: | $\boldsymbol{y}$ |
| :--- | :--- | :--- |
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## Lesson Summary

A linear equation in two-variables $x$ and $y$ is in standard form if it is of the form $a x+b y=c$ for numbers $a, b$, and $c$, where $a$ and $b$ are both not zero. The numbers $a, b$, and $c$ are called constants.

A solution to a linear equation in two variables is the ordered pair $(x, y)$ that makes the given equation true. Solutions can be found by fixing a number for $x$ and solving for $y$ or fixing a number for $y$ and solving for $x$.

## Problem Set

1. Consider the linear equation $x-\frac{3}{2} y=-2$.
a. Will you choose to fix values for $x$ or $y$ ? Explain.
b. Are there specific numbers that would make your computational work easier? Explain.
c. Find five solutions to the linear equation $x-\frac{3}{2} y=-2$, and plot the solutions as points on a coordinate plane.

| $\boldsymbol{x}$ | Linear Equation: <br> $x-\frac{3}{2} y=-2$ | $\boldsymbol{y}$ |
| :--- | :--- | :--- |
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2. Find five solutions for the linear equation $\frac{1}{3} x+y=12$, and plot the solutions as points on a coordinate plane.
3. Find five solutions for the linear equation $-x+\frac{3}{4} y=-6$, and plot the solutions as points on a coordinate plane.
4. Find five solutions for the linear equation $2 x+y=5$, and plot the solutions as points on a coordinate plane.
5. Find five solutions for the linear equation $3 x-5 y=15$, and plot the solutions as points on a coordinate plane.
