## Lesson 13: Angle Sum of a Triangle

## Classwork

## Concept Development



$$
m \angle 1+m \angle 2+m \angle 3=m \angle 4+m \angle 5+m \angle 6=m \angle 7+m \angle 8+m \angle 9=180^{\circ}
$$

Note that the sum of the measures of angles 7 and 9 must equal $90^{\circ}$ because of the known right angle in the right triangle.

## Exploratory Challenge 1

Let triangle $A B C$ be given. On the ray from $B$ to $C$, take a point $D$ so that $C$ is between $B$ and $D$. Through point $C$, draw a segment parallel to $\overline{A B}$, as shown. Extend the segments $A B$ and $C E$. Line $A C$ is the transversal that intersects the parallel lines.

a. Name the three interior angles of triangle $A B C$.
b. Name the straight angle.
c. What kinds of angles are $\angle A B C$ and $\angle E C D$ ? What does that mean about their measures?
d. What kinds of angles are $\angle B A C$ and $\angle E C A$ ? What does that mean about their measures?
e. We know that $m \angle B C D=m \angle B C A+m \angle E C A+m \angle E C D=180^{\circ}$. Use substitution to show that the measures of the three interior angles of the triangle have a sum of $180^{\circ}$.

## Exploratory Challenge 2

The figure below shows parallel lines $L_{1}$ and $L_{2}$. Let $m$ and $n$ be transversals that intersect $L_{1}$ at points $B$ and $C$, respectively, and $L_{2}$ at point $F$, as shown. Let $A$ be a point on $L_{1}$ to the left of $B, D$ be a point on $L_{1}$ to the right of $C, G$ be a point on $L_{2}$ to the left of $F$, and $E$ be a point on $L_{2}$ to the right of $F$.

a. Name the triangle in the figure.
b. Name a straight angle that will be useful in proving that the sum of the measures of the interior angles of the triangle is $180^{\circ}$.
c. Write your proof below.

## Lesson Summary

All triangles have a sum of measures of the interior angles equal to $180^{\circ}$.
The proof that a triangle has a sum of measures of the interior angles equal to $180^{\circ}$ is dependent upon the knowledge of straight angles and angle relationships of parallel lines cut by a transversal.

## Problem Set

1. In the diagram below, line $A B$ is parallel to line $C D$, that is, $L_{A B} \| L_{C D}$. The measure of $\angle A B C$ is $28^{\circ}$, and the measure of $\angle E D C$ is $42^{\circ}$. Find the measure of $\angle C E D$. Explain why you are correct by presenting an informal argument that uses the angle sum of a triangle.

2. In the diagram below, line $A B$ is parallel to line $C D$, that is, $L_{A B} \| L_{C D}$. The measure of $\angle A B E$ is $38^{\circ}$, and the measure of $\angle E D C$ is $16^{\circ}$. Find the measure of $\angle B E D$. Explain why you are correct by presenting an informal argument that uses the angle sum of a triangle. (Hint: Find the measure of $\angle C E D$ first, and then use that measure to find the measure of $\angle B E D$.)

3. In the diagram below, line $A B$ is parallel to line $C D$, that is, $L_{A B} \| L_{C D}$. The measure of $\angle A B E$ is $56^{\circ}$, and the measure of $\angle E D C$ is $22^{\circ}$. Find the measure of $\angle B E D$. Explain why you are correct by presenting an informal argument that uses the angle sum of a triangle. (Hint: Extend the segment $B E$ so that it intersects line $C D$.)

4. What is the measure of $\angle A C B$ ?

5. What is the measure of $\angle E F D$ ?

6. What is the measure of $\angle H I G$ ?

7. What is the measure of $\angle A B C$ ?

8. Triangle $D E F$ is a right triangle. What is the measure of $\angle E F D$ ?

9. In the diagram below, Lines $L_{1}$ and $L_{2}$ are parallel. Transversals $r$ and $s$ intersect both lines at the points shown below. Determine the measure of $\angle J M K$. Explain how you know you are correct.

