## Lesson 3: Numbers in Exponential Form Raised to a Power

## Classwork

For any number $x$ and any positive integers $m$ and $n$,

$$
\left(x^{m}\right)^{n}=x^{n m}
$$

because

$$
\begin{aligned}
\left(x^{m}\right)^{n} & =\underbrace{(x \cdot x \cdots x)^{n}}_{m \text { times }} \\
& =\underbrace{(x \cdot x \cdots x)}_{n \text { times }} \times \cdots \times \underbrace{(x \cdot x \cdots x)}_{m \text { times }} \\
& =x^{n m} .
\end{aligned}
$$

## Exercise 1

$\left(15^{3}\right)^{9}=$

## Exercise 2

$\left((-2)^{5}\right)^{8}=$

## Exercise 3

$\left(3.4^{17}\right)^{4}=$

## Exercise 4

Let $s$ be a number.
$\left(s^{17}\right)^{4}=$

## Exercise 5

Sarah wrote $\left(3^{5}\right)^{7}=3^{12}$. Correct her mistake. Write an exponential equation using a base of 3 and exponents of 5, 7, and 12 that would make her answer correct.

## Exercise 6

A number $y$ satisfies $y^{24}-256=0$. What equation does the number $x=y^{4}$ satisfy?

For any numbers $x$ and $y$, and positive integer $n$,

$$
(x y)^{n}=x^{n} y^{n}
$$

because

$$
\begin{aligned}
(x y)^{n} & =\underbrace{(x y) \cdots(x y)}_{n \text { times }} \\
& =\underbrace{(x \cdot x \cdots x)}_{n \text { times }} \cdot \underbrace{(y \cdot y \cdots y)}_{n \text { times }} \\
& =x^{n} y^{n} .
\end{aligned}
$$

## Exercise 7

$(11 \times 4)^{9}=$

## Exercise 10

Let $x$ be a number.
$(5 x)^{7}=$

## Exercise 11

Let $x$ and $y$ be numbers.
$\left(5 x y^{2}\right)^{7}=$

## Exercise 9

Let $a, b$, and $c$ be numbers.
$\left(3^{2} a^{4}\right)^{5}=$

## Exercise 12

Let $a, b$, and $c$ be numbers.

$$
\left(a^{2} b c^{3}\right)^{4}=
$$

## Exercise 13

Let $x$ and $y$ be numbers, $y \neq 0$, and let $n$ be a positive integer. How is $\left(\frac{x}{y}\right)^{n}$ related to $x^{n}$ and $y^{n}$ ?

## Problem Set

1. Show (prove) in detail why $(2 \cdot 3 \cdot 7)^{4}=2^{4} 3^{4} 7^{4}$.
2. Show (prove) in detail why $(x y z)^{4}=x^{4} y^{4} z^{4}$ for any numbers $x, y, z$.
3. Show (prove) in detail why $(x y z)^{n}=x^{n} y^{n} z^{n}$ for any numbers $x, y$, and $z$ and for any positive integer $n$.
